

Theory of Muon $g - 2$

Joaquim Prades

CAFPE and Universidad de Granada

Workshop on Low Energy Constraints
on Extensions of the Standard Model,

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Kazimierz



Plan

⇒ Introduction: Electron $g - 2$

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- ⇒ Main Contribution to $g - 2$: QED

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- ⇒ Hadronic Contributions to Muon $g - 2$

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- ⇒ Electroweak Contribution to Muon $g - 2$
- ⇒ Hadronic Contributions to Muon $g - 2$
- ⇒ Conclusions and Prospects

Introduction

Fermion–External EM Field $A^\mu(q = p - p')$ Vertex

$$\bar{u}(p')\Gamma_\mu u(p) = \bar{u}(p') \left[\gamma_\mu F_1(q^2) + i \frac{\sigma_{\mu\nu} q^\nu}{2m_l} F_2(q^2) + \dots \right] u(p)$$

Magnetic Dipole Moment for Charged Fermion ($l = e, \mu, \tau, \dots$)

$$\vec{\mu} = g_l \frac{e}{2m_l} \vec{s} \quad \text{with} \quad g_l \equiv 2 (F_1(0) + F_2(0))$$

Dirac Vertex Prediction

Tree-Level: $F_1(0) = 1$ and $F_2(0) = 0$

Quantum Loops: $F_1(0) = 1$ and $a_l \equiv F_2(0) \neq 0$

The Electron Anomaly

Very Recent Measurement of a_e :

2006-2008 Harvard group: $a_e^{\text{exp}} = (11\,596\,521\,807.3 \pm 2.8) 10^{-13}$

1987 Univ. of Washington group:

$a_e^{\text{exp}} = (11\,596\,521\,883 \pm 42) 10^{-13}$ Factor 15 of improvement !!

α_{QED} : one order of magnitude more precise !

$\alpha^{-1} = 137.035\,999\,084(33)(39) = 137.035\,999\,084(51)$

than previous determinations

Cs atom (2002): $\alpha^{-1} = 137.036\,000\,000(1100)$

Rb atom (2006): $\alpha^{-1} = 137.035\,998\,780(910)$

Wrong: Based on a_e 2007

PDG 2008 (CODATA 2006): $\alpha^{-1} = 137.035\,999\,679(94)$

Main Contribution: QED

$$a_e^{\text{QED}} = \sum_{n=1} C_{2n} \left(\frac{\alpha}{\pi}\right)^n$$

$C_2 = 1/2$: Schwinger •

C_4 : Analytical including lepton mass corrections •

Sommerfield; Petermann; Suura, Wichmann; Elend; Passera

C_6 : Analytical including lepton mass corrections •

Kinoshita, Barbieri, Laporta, Remiddi, ...

C_8 : Numerical (Revised value in 2007) •

Kinoshita, Nio, Aoyama, Hayakawa

$C_{10} = (0.0 \pm 4.6)$: Estimate (Calculation in progress 12672 diagrams) •

Kinoshita, Nio, Aoyama, Hayakawa

★ Aguilar, Greynat, de Rafael (specific class of eight and tenth order analytically)

Hadronic and EW Contributions

Hadronic Contribution

$$a_e^{\text{LO Hadronic}} = (16.71 \pm 0.19) 10^{-13}; \quad a_e^{\text{HLbL}} = (0.35 \pm 0.10) 10^{-13}$$

Davier, Höcker; Krause; Knecht

J.P., de Rafael, Vainshtein

First Time a_e^{exp} Sensitive to Hadronic Contribution 6σ !

One-loop electroweak contribution not yet needed ●

$$a_e^{\text{EW}} = (0.297 \pm 0.005) \times 10^{-13}$$

At present:

a_e together with α from Rb and Cs checks QED at 3-loops ●

If comparable uncertainty in α :

Checks QED to 4-loops and electron substructure ●

The Muon Anomaly: QED

Impressive achievement BNL Muon (g-2) Collaboration:

$$a_{\mu}^{\text{exp}} = (11\,659\,208.0 \pm 5.4 \pm 3.3) 10^{-10} = (11\,659\,208.0 \pm 6.3) 10^{-10}$$

Standard Model Prediction: QED

$$a_{\mu}^{\text{QED}} = \sum_{n=1} C_{2n} \left(\frac{\alpha}{\pi}\right)^n$$

$C_2 = 1/2$: Schwinger •

C_4 : Analytical including lepton mass corrections •

Sommerfield; Petermann; Suura, Wichmann; Elend; Passera

C_6 : Analytical including lepton mass corrections •

Kinoshita, Barbieri, Laporta, Remiddi, . . .

The Muon Anomaly: QED

C_8 : Numerical value (revised in 2007) •

Kinoshita, Nio, Aoyama, Hayakawa

$C_{10} = (663 \pm 20)$: Estimate

(Calculation in progress 12672 diagrams) •

Kinoshita, Nio, Aoyama, Hayakawa

Using α from a_e $\Rightarrow a_\mu^{\text{QED}} = (11\,658\,471.810 \pm 0.015) \times 10^{-10}$

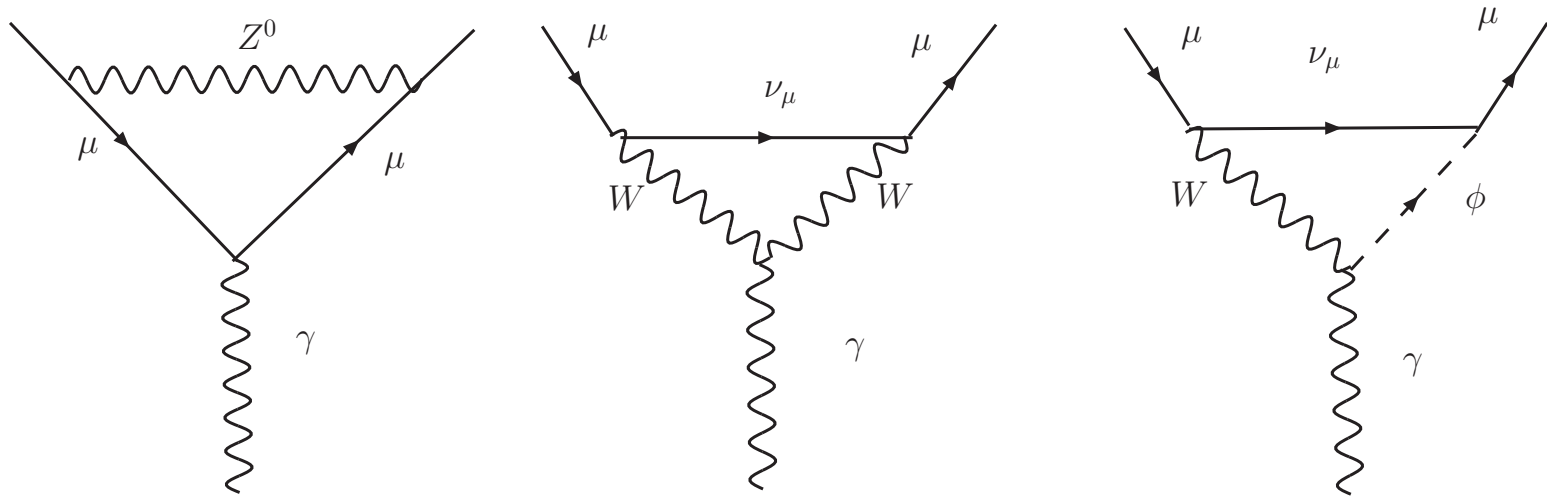
Uncertainty dominated by C_{10} •

$$\Delta_{\text{Not QED}}^{\text{exp}} = (736.2 \pm 6.3) \times 10^{-10}$$

Sensitive to hadronic contribution since 1975 and to electroweak contribution since 2001 •

Electroweak Contribution

At one-loop,

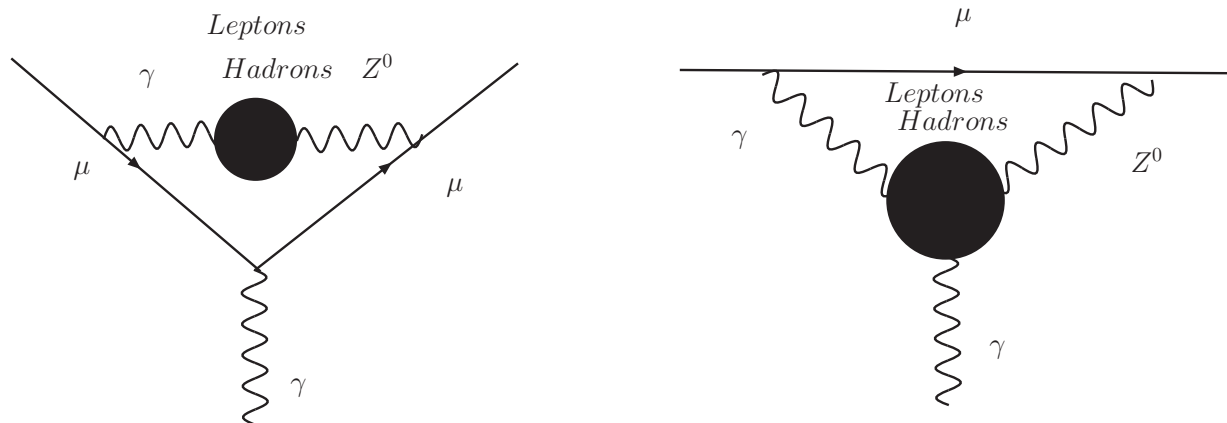


$$a_{\mu}^{\text{EW}} = \frac{5G_{\mu}m^2}{24\sqrt{2}\pi^2} \left[1 + \frac{1}{5} (1 - 4\sin^2(\theta_W))^2 + \mathcal{O}(m/M_{Z,W,H})^2 \right]$$

1972: Jackiw, Weinberg; Bars, Yoshimura; Altarelli, Cabibbo, Maiani; Bardeen, Gastmans, Lautrup; Fujikawa, Lee, Sanda

Electroweak Contribution

Including Two-Loops Electroweak: 1992-2004



Kukhto et al.; Czarnecki, Krause, Marciano, Vainshtein; Knecht, Peris, Perrottet, de Rafael; Degrossi, Giudice; Heinemeyer, Stöckinger, Weiglein

Need full Standard Model anomaly cancellation •

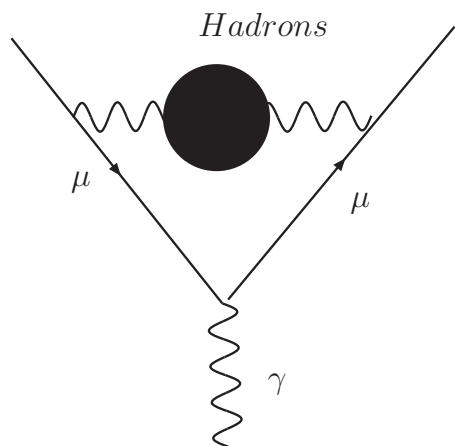
Vainshtein 2003 New renormalization theorem hadronic $\langle VVA \rangle$ •

$$a_{\mu}^{\text{EW}} = [(19.5 \pm 0.2) - (4.1 \pm 0.1)] 10^{-10} = (15.4 \pm 0.2) 10^{-10}$$

Hadronic Vacuum Polarization

$$\Delta_{\text{Not QED+EW}}^{\text{exp}} = (720.8 \pm 6.3) \times 10^{-10} \Rightarrow$$

Need hadronic contribution with accuracy smaller than 1 % •



$$a_{\mu}^{\text{LO Hadronic}} = \frac{1}{4\pi^3} \int_{4m_{\pi}^2}^{\infty} ds K(s) \sigma^{(0)}(s)$$

$$K(s) = \int_0^1 dx \frac{x^2(1-x)}{x^2 + \frac{s}{m^2}(1-x)}$$

$\sigma^{(0)}(s)$ is the one-photon $e^+e^- \rightarrow \gamma^* \rightarrow$ hadrons cross-section •

Bouchiat, Michel; Gourdin, de Rafael

Hadronic Vacuum Polarization

$\sigma^{(0)}(s)$ is (almost) experimentally obtained •

Radiative corrections:

Include final state photons but

exclude $\alpha(q^2)$ running (double counting) in σ^0 •

Use QCD: At high energy (≥ 13 GeV) and

in between $\bar{c}c$ and $\bar{b}b$ thresholds ✓

$K(s)$ goes as m^2/s \Rightarrow low energy (ρ -region) dominates •

$\pi^+\pi^-$ channel below 1 GeV gives 72 % of the total ✓

Hadronic Vacuum Polarization

Very precise e^+e^- data:

CMD-2 and SND at VEPP-2M (Novosibirsk) and KLOE at DAΦNE (Frascati) ✓

CMD-2 and SND in agreement ✓

KLOE: same level of accuracy and reasonable overall agreement between 0.630 and 0.958 GeV with CMD-2 and SND though lies somewhat lower ✓

Also BaBar has released first exclusive e^+e^- data ✓

Belle larger statistics, soon

Hadronic Vacuum Polarization

Authors	Contribution $\times 10^{10}$
Davier et al., τ data (2003)	$711.0 \pm 5.0_{\text{exp}} \pm 0.8_{\text{rad}} \pm 2.4_{\text{IB}}$
de Tróconiz, Ynduráin, τ data (2004)	$702.7 \pm 4.7_{\text{exp}} \pm 1.0_{\text{rad}}$
Davier et al., τ data (2009)	$704.4 \pm 3.5_{\text{exp}} \pm 0.7_{\text{rad}} \pm 1.9_{\text{IB}}$
Davier et al. e^+e^- (2006)	$690.8 \pm 3.0_{\text{exp}} \pm 1.9_{\text{rad}} \pm 0.7_{\text{QCD}}$
Hagiwara et al. e^+e^- (2006)	$689.4 \pm 4.2_{\text{exp}} \pm 1.8_{\text{rad}}$
Jegerlehner e^+e^- (2006)(without KLOE)	692.1 ± 5.6
Jegerlehner e^+e^- (2008)	690.3 ± 5.3
Davier et al. e^+e^- (2009)	$689.1 \pm 3.8_{\text{exp}} \pm 1.9_{\text{rad}} \pm 0.7_{\text{QCD}}$
Davier et al. e^+e^- (2009) (without KLOE)	$690.1 \pm 4.6_{\text{exp}} \pm 1.9_{\text{rad}} \pm 0.7_{\text{QCD}}$

Hadronic Vacuum Polarization

New IB analysis including Belle data (Davier et al (2009)):

τ data vs e^+e^- smaller data discrepancy:

previous $4.5 \sigma \Rightarrow (1.6 \sim 2.7) \sigma$ in $(B_\tau - B_{\text{CVC}})_{\pi+\pi^0}$ ✓

New accurate e^+e^- data agree reasonably within them ✓

SU(2)-isospin effects could be larger than expected:

Much less theory involved in e^+e^- data ●

Most recent evaluations include SND, CMD-2,

(before 2008) BaBar and KLOE data: 0.6 % accuracy !

$$a_\mu^{\text{LO Hadronic}} = (689.1 \pm 4.3) \times 10^{-10}$$

Upcoming VEPP-2000 and DAΦNE-2 (normalized to $\mu^+\mu^-$) ✓

Hadronic Vacuum Polarization

That was the situation before Tau 2008 at Novosibirsk

⇒ Preliminary BaBar $e^+e^- \rightarrow \pi^+\pi^-(\gamma)$ cross section between (0.5, 3.0) GeV presented (M. Davier) •

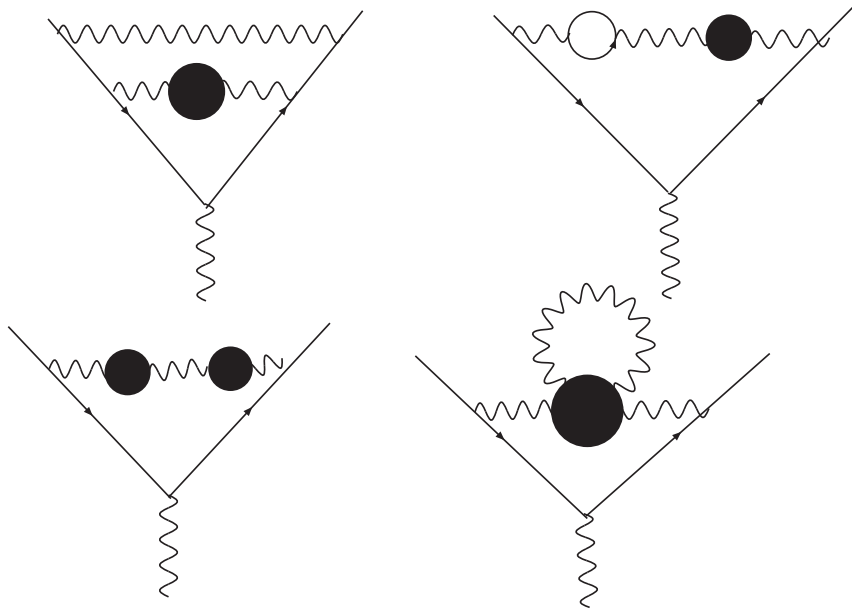
★ Disagreement with CMD-II and SND below the ρ and most notably with 2008 KLOE analysis between (0.5, 1.0) GeV ??

★ Agree better with tau data, especially with Belle and CLEO but still some disagreement with ALEPH •

★ If BaBar is the only used in (0.5,1.8) GeV the result is 3σ away the previous e^+e^- “world average” !

★★ Caution Preliminary: Wait to final results (in two weeks !) !
no higher multi-hadronic modes included •

Higher Order Hadronic



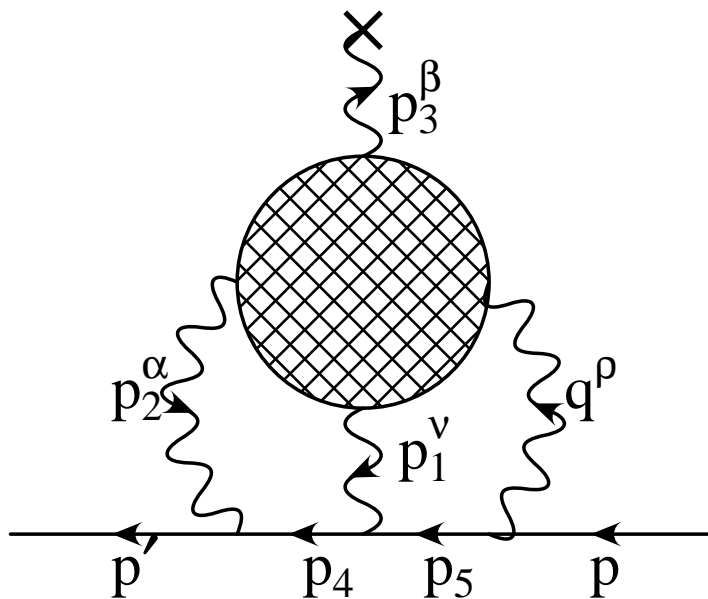
At order α^3 : using same e^+e^- data as for LO •

$$a_{\mu}^{\text{HO Hadronic}} = -(9.79 \pm 0.10) \times 10^{-10}$$

Uncertainty includes unaccounted radiative corrections •

Hadronic Light-by-Light Scattering

Hadronic light-by-light contribution to muon $g - 2$



$$\mathcal{M} = |e|^7 \beta \int \frac{d^4 p_1}{(2\pi)^4} \int \frac{d^4 p_2}{(2\pi)^4} \frac{1}{q^2 p_1^2 p_2^2 (p_4^2 - m^2) (p_5^2 - m^2)} \\ \times \underline{\Pi^{\rho\nu\alpha\beta}(p_1, p_2, p_3)} \bar{u}(p') \gamma_\alpha (\not{p}_4 + m) \gamma_\nu (\not{p}_5 + m) \gamma_\rho u(p)$$

Introduction

Need

$$\Pi^{\rho\nu\alpha\beta}(p_1, p_2, p_3) = i^3 \int d^4x \int d^4y \int d^4z \exp^{i(p_1 \cdot x + p_2 \cdot y + p_3 \cdot z)} \times \\ \times \langle 0 | T [V^\rho(0) V^\nu(x) V^\alpha(y) V^\beta(z)] | 0 \rangle$$

with $V^\mu(x) = [\bar{q} \hat{Q} \gamma^\mu q](x)$ and $\hat{Q} = \frac{1}{3} \text{diag}(2, -1, -1)$

full four-point function with $p_3 \rightarrow 0$ •

Using current conservation

$$\Pi^{\rho\nu\alpha\lambda}(p_1, p_2, p_3) = -p_{3\beta} \frac{\delta \Pi^{\rho\nu\alpha\beta}(p_1, p_2, p_3)}{\delta p_{3\lambda}}$$

one just needs derivatives at $p_3 = 0$ •

Introduction

★ Many scales involved: Impose low energy and several OPE limits \Rightarrow Not full first principle calculation at present ●

(Two lattice groups just starting: Not clear final uncertainty) ●

Large N_c and CHPT counting:

Organizes different degrees of freedom contributions ●

E. de Rafael

- Goldstone boson exchange: $\mathcal{O}(N_c)$ and $\mathcal{O}(p^6)$ ●
- One-meson irreducible vertex and non-Goldstone boson exchange: $\mathcal{O}(N_c)$ and $\mathcal{O}(p^8)$ ●
- Goldstone bosons Loop: $\mathcal{O}(1)$ in $1/N_c$ and $\mathcal{O}(p^4)$ ●
- Non-Goldstone bosons Loop: $\mathcal{O}(1)$ in $1/N_c$ and $\mathcal{O}(p^8)$ ●

Introduction

Based on this counting:

- Two full calculations
J. Bijnens, E. Pallante, J.P. (BPP)
M. Hayakawa, T. Kinoshita, A. Sanda (HKS)
- Dominant pseudo-scalar exchange: Extensive analytic analysis ●
M. Knecht, A. Nyffeler (KN)

Found sign mistake ✓

M. Knecht, A. Nyffeler, M. Perrottet, E. de Rafael

Introduction

★ New four-point form factor short-distance constraint:

K. Melnikov, A. Vainshtein

(see also M. Knecht, S. Peris, M. Perrottet, E. de Rafael)

Model:

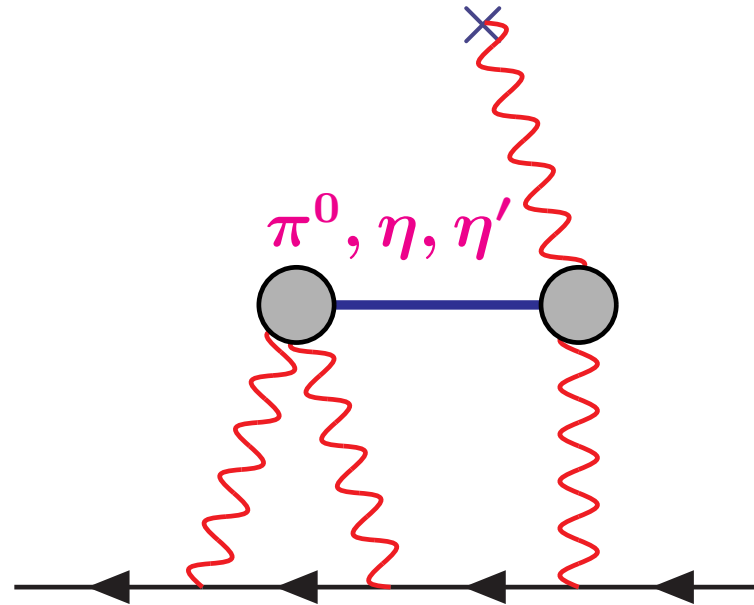
Full light-by-light saturated by pseudo-scalar and pseudo-vector pole exchanges ●

Very recently, A. Nyffeler used a $\pi^0 \gamma^* \gamma^*$ off-shell form factor ●

First step, one needs more work to have the full light-by-light ●

“Old” Calculations: Pseudo-Scalar Exchange

Dominant contribution \Rightarrow pseudo-scalar exchange •



Nambu-Goldstone π^0 makes special enhancement •

$$a(\pi^0) = \left(\frac{\alpha}{\pi}\right)^3 N_c \frac{m^2 N_c}{48\pi^2 f_\pi^2} \left[\ln^2 \frac{M_\rho}{m_\pi} + \mathcal{O}\left(\ln \frac{M_\rho}{m_\pi}\right) + \mathcal{O}(1) \right]$$

M. Knecht, A. Nyffeler, M. Perrottet, E. de Rafael

“Old” Calculations: Pseudo-Scalar Exchange

Here, I discuss work in J. Bijnens, E. Pallante, J.P. •
We used a variety of $\pi^0 \gamma^* \gamma^*$ form factors

$$\mathcal{F}^{\mu\nu}(p_1, p_2) = \frac{N_c}{6\pi} \frac{\alpha}{f_\pi} i\varepsilon^{\mu\nu\alpha\beta} p_{1\alpha} p_{2\beta} \underline{\mathcal{F}(p_1^2, p_2^2)}$$

fulfilling as many as possible QCD constraints •
(Short-distance, data, $U_A(1)$ normalization and slope at the origin). In particular,

$$\begin{aligned} \mathcal{F}(Q^2, Q^2) &\rightarrow \frac{A}{Q^2} \\ \mathcal{F}(Q^2, 0) &\rightarrow \frac{B}{Q^2} \end{aligned}$$

for Q^2 Euclidean and very large

“Old” Calculations: Pseudo-Scalar Exchange

All form factors we used converge for $\mu \sim (2 - 4)$ GeV and the numerical difference between them is small ✓

Somewhat different $\pi^0 \gamma^* \gamma^*$ form factors used in
M. Hayakawa, T. Kinoshita, A. Sanda and M. Knecht, A. Nyffeler •

Results agree very well (after correcting a mistake in the sign of the phase space) •

	$10^{10} \times a_\mu$
Adding π^0 , η and η' contributions	BPP (8.5 ± 1.3)
	HKS (8.3 ± 0.6)
	KN (8.3 ± 1.2)

“Old” Calculations: Pseudo-Vector Exchange

Need $f_1\gamma\gamma^*$ and $f_1\gamma^*\gamma^*$ form factors •

⇒ related to $\pi^0\gamma\gamma^*$ and $\pi^0\gamma^*\gamma^*$ by anomalous Ward identities ✓

Pseudo-vector exchange

	$10^{10} \times a_\mu$
BPP	(0.25 ± 0.10)
HKS	(0.17 ± 0.10)

“Old” Calculations: Scalar Exchange

Need $S^0\gamma\gamma^*$ and $S^0\gamma^*\gamma^*$ form factors •

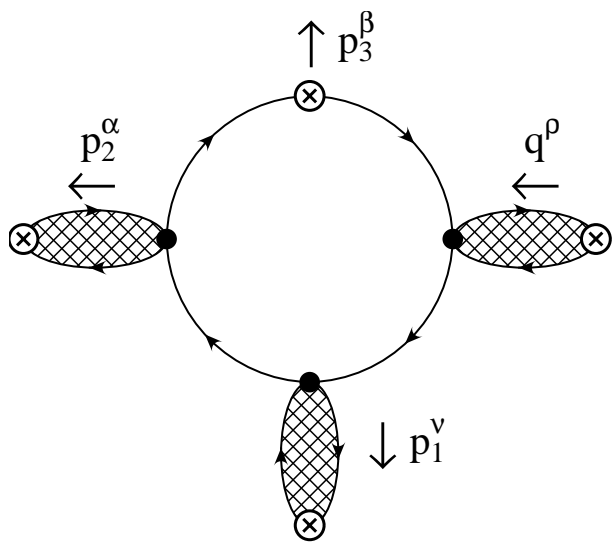
They are constrained by CHPT at $\mathcal{O}(p^4)$: L_i 's reproduced ✓

Within ENJL: Ward identities impose relations between
Quark loop and Scalar exchange •

$$a_\mu(\text{Scalar}) = -(0.7 \pm 0.2) \times 10^{-10}$$

Not included by M. Hayakawa, T. Kinoshita and A. Sanda
nor by K. Melnikov and A. Vainshtein •

“Old” Calculations: Non-Meson Exchange “Quark-Loop”

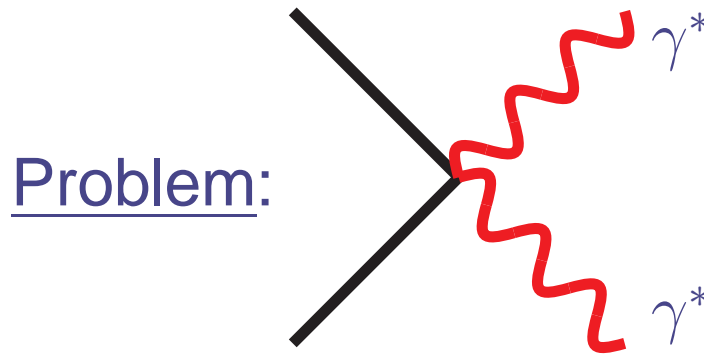
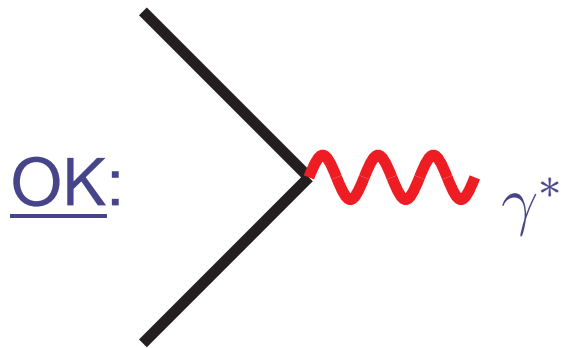


Λ [GeV]	$10^{10} \times a_\mu$
0.7	2.2
1.0	2.0
2.0	1.9
4.0	2.0

- Low Energy (0 to Λ): ENJL model ●
- High Energy (Λ to ∞): Short-distance QCD bare quark loop ●
- Numerical matching ✓

“Old” Calculations: Pion- and Kaon-Loop

Leading contribution in chiral counting, suppressed by $1/N_c$



No $\gamma^* \gamma^* \rightarrow \pi\pi$ data available: Models needed !

Model for $\pi\pi\gamma^*(\gamma^*)$	$10^{10} \times a_\mu$
BPP (Full VMD)	-1.8
HKS (HGS)	-0.4
No Photon Form Factor	-4.6

Kaon loop is much smaller: -0.05×10^{-10} ●

New Short Distance Constraints

K. Melnikov and A. Vainshtein

New short-distance constraint on four-point function form factor

$$\langle 0 | T [V^\nu(p_1) V^\alpha(p_2) V^\rho(-(p_1 + p_2 + p_3))] | \gamma(p_3 \rightarrow 0) \rangle$$

using OPE with $-p_1^2 \simeq -p_2^2 \gg -(p_1 + p_2)^2$ Euclidean and large,

$$T[V^\nu(p_1) V^\alpha(p_2)] \sim \frac{1}{\hat{p}^2} \varepsilon^{\nu\alpha\mu\beta} \hat{p}_\mu [\bar{q} \hat{Q}^2 \gamma_\beta \gamma_5 q](p_1 + p_2)$$

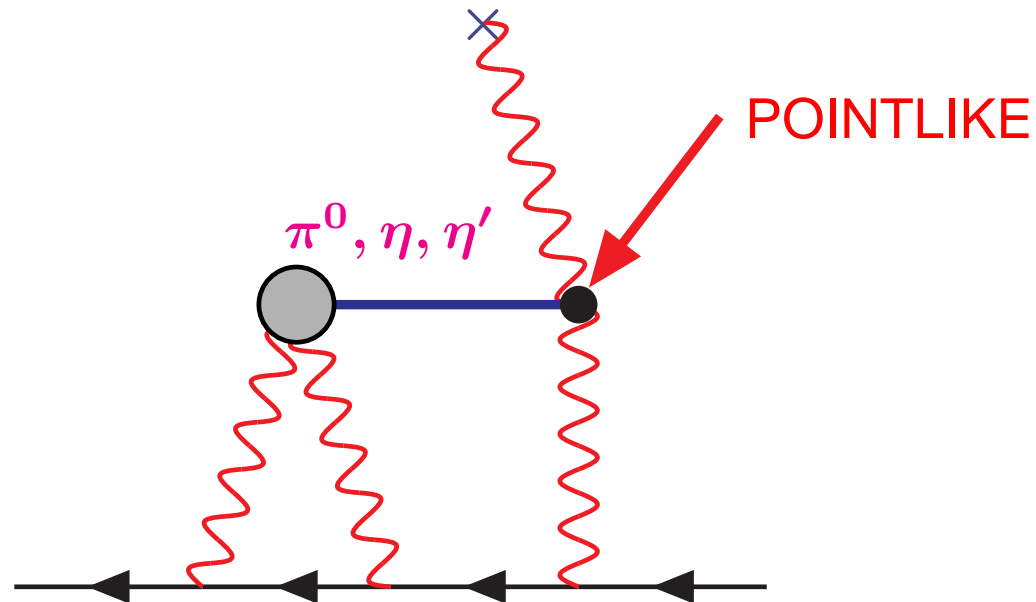
with $\hat{p} = (p_1 - p_2)/2 \simeq p_1 \simeq -p_2$

New OPE Constraint: Pseudo-scalar exchange

New OPE constraint saturated by pseudo-scalar exchange

⇒ Model uses a point-like vertex when $p_3 \rightarrow 0$ •

Not all OPE constraints satisfied: Negligible numerically •



New OPE Constraint: Axial-Vector exchange

Axial-Vector exchange depends very much on the resonance mass mixing •

K. Melnikov and A. Vainsthein:

Ideal mixing for $f_1(1285)$ and $f_1(1420)$ •

Mass mixing	$10^{10} \times a_\mu$
No New OPE (Nonet symmetry)	0.3 ± 0.1
M=1.3 GeV (Nonet symmetry)	0.7
M= M_ρ (Nonet symmetry)	2.8
Ideal mixing	2.2 ± 0.5

Comparison: Leading order in N_c

Leading order in N_c :

Quark Loop + Pseudo-Scalar + Pseudo-Vector + Scalar Exchanges •

Total at $\mathcal{O}(N_c)$	$10^{10} \times a_\mu$
BPP (Nonet symmetry)	$(10.9 \pm 1.9) + \underline{-(0.7 \pm 0.1)} = (10.2 \pm 1.9)$
HKS (Nonet symmetry)	$(9.4 \pm 1.6) + ??\text{Scalar}??$

MV: Hadronic model saturated by pole exchanges:

Cannot compare individual contributions •

Total at $\mathcal{O}(N_c)$	$10^{10} \times a_\mu$
MV (Nonet symmetry)	$(12.1 \pm 1.0) + ??\text{Scalar}??$
MV (Ideal mass mixing)	$(13.6 \pm 1.5) + ??\text{Scalar}??$

Masses produce main difference in pseudo-vector exchange •

Conclusions and Prospects

At present, large N_c results agree within 1σ ✓

$$a_{\mu}^{N_c, \text{HLbL}} = (11.0 \pm 4.0) \times 10^{-10}$$

Based partly in this discussion: Recent new analysis of HLbL

J.P., E. de Rafael and A. Vainshtein

★ $1/N_c$ expansion works reasonably well ✓

★ Chiral enhancement factors demand more than the lightest Nambu-Goldstone bosons ●

Conclusions Prospects

Adding effects beyond leading order in $1/N_c$, in a conservative analysis, **J.P., E. de Rafael and A. Vainshtein**

π^0 , η and η' exchanges: $(11.4 \pm 1.3) \times 10^{-10}$
(includes non-meson exchange in ENJL case)

Scalar exchange : $-(0.7 \pm 0.7) \times 10^{-10}$

Axial-vector exchange : $(1.5 \pm 1.0) \times 10^{-10}$

Pion and kaon loops: $-(1.9 \pm 1.9) \times 10^{-10}$

Charm quark loop: 0.23×10^{-10}

★ Our final result is $a_\mu^{\text{HLbL}} = (10.5 \pm 2.6) \times 10^{-10}$

Standard Model Prediction of a_μ

$$\begin{aligned}
 10^{10} a_\mu^{\text{SM}} &= \overbrace{(11\,658\,471.810 \pm 0.015)}^{\text{QED}} + \overbrace{(15.4 \pm 0.2)}^{\text{EW}} + \\
 &+ \underbrace{(689.1 \pm 4.3)}_{\text{LO Had}} - \underbrace{(9.79 \pm 0.10)}_{\text{HO Had}} + \underbrace{(10.5 \pm 2.6)}_{\text{HLbL}} \\
 &= \underbrace{(11\,658\,487.2 \pm 0.2)}_{\text{QED + EW}} + \underbrace{(689.8 \pm 5.0)}_{\text{Hadronic}} \\
 &= \underline{(11\,659\,177.0 \pm 5.0)}
 \end{aligned}$$

Theory error smaller than experiment error ✓

$$\begin{aligned}
 a_\mu^{\text{exp}} - a_\mu^{\text{SM}} &= (31.0 \pm 8.1) \times 10^{-10} \Rightarrow \underline{3.8 \sigma} \\
 a_\mu^{\text{exp}} - a_\mu^{\text{SM}} &= (30.0 \pm 8.5) \times 10^{-10} \Rightarrow \underline{3.5 \sigma} \text{ (without KLOE)}
 \end{aligned}$$

Prospects for Theory and Experiment

New e^+e^- experiments:

cross-checks and reduce final uncertainty of $a_\mu^{\text{LO Had}}$ ●

New τ data at B-factories and new tau-charm factory at Beijing:
cross-checks with actual tau data ●

Recall the preliminary (and partial) BaBar result ●

Need theoretical understanding isospin violation to use τ data ●

A new full calculation of a_μ^{HLbL} is desirable and possible: Goal:
 $\sim (1.5 - 2.0) \times 10^{-10}$ uncertainty in a_μ^{HLbL} ●

Prospects for total theory uncertainty: $\sim 3.5 \times 10^{-10}$ ●

Prospects for Theory and Experiment

A tantalizing discrepancy $(3.5 \sim 3.8) \sigma$ and expectations to reduce theory uncertainty ✓

★ New $g - 2$ experiment at Fermilab approved but not funded yet

⇒: reduces the E861 uncertainty from 6.3×10^{-10} to 1.6×10^{-10}



★ J-PARC project (Japan) goal: reduce it even more !

⇒ Very timely: Make new (\$ 55 Million at FNAL)

experiment to measure a_μ

May become first new physics discovery !